

(I)

Terminating Decimals If the decimal expression of a/b terminates i.e. comes to end, then the decimal so obtained is called terminating decimals. [or non repeating decimals]

Example = $\frac{1}{4} = 0.25$

Repeating Decimal - A decimal in which a digit or a set of digits repeats repeatedly periodically is called a repeating decimal.

Example = $\frac{2}{3} = 0.666\dots$

Some Special Characteristics of Rational Numbers -

- Every rational number is expressible either as a terminating decimal or as a repeating decimal.
- Every terminating decimal is a rational number.
- Every repeating decimal is a rational number.

Irrational Numbers :- (i) The non terminating, non repeating decimals are called irrational numbers.

Example = $0.010012111200\dots$

(ii) Similarly, if m is a positive number which is not a perfect square, then \sqrt{m} is also irrational.

Example = $\sqrt{3}, \sqrt{5}, \sqrt{7}$ etc.

(iii) If m is a positive integer which is not a perfect cube, then $\sqrt[3]{m}$ is irrational.

Example - $\sqrt[3]{2}$

(2)

Properties of Irrational Numbers :-

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(i) These satisfy the commutative, associative and distributive laws for addition and multiplication.

(ii) Sum of two irrationals need not be irrational.

Example = $(5 + \sqrt{2}) - (3 + \sqrt{2}) = 2$

(iii) Product of two irrationals need not be irrational.

Example = $\sqrt{3} \times \sqrt{3} = 3$

(iv) The quotient of two irrationals need not be irrational.

Example = $\frac{2\sqrt{3}}{\sqrt{3}} = 2$

(v) Sum of rational and irrational is irrational.

Example = $(2 + \sqrt{3})$

(vi) The difference of a rational number and an irrational number is irrational.

Example = $(8 - \sqrt{5})$ is an irrational.

(vii) Product of rational and irrational is irrational.

Example = $3 \times \sqrt{2}$ is an irrational.

(viii) Quotient of Rational and irrational is irrational.

Example = $\frac{3}{\sqrt{3}}$ is an irrational.

RATIONALISATION If we have an irrational number, then the process of converting the denominator to a rational number by multiplying the numerator and denominator by a suitable number, is called rationalization.

Example - $\frac{3}{\sqrt{2}} = \frac{3 \times \sqrt{2}}{\sqrt{2} \times \sqrt{2}} = \frac{3\sqrt{2}}{2}$

Laws of Radicals -

Let $a > 0$ be a real number, and let p and q be rational numbers, then we have

$$(I) \quad a^p \times a^q = a^{(p+q)}$$

$$(II) \quad (a^p)^q = a^{pq}$$

$$(III) \quad a^p / a^q = a^{(p-q)}$$

$$(IV) \quad a^p \times b^p = (ab)^p$$

Now - Exercise - 1.2

Que ① State whether the following statements are true or false. Justify also your answer

(I) Every irrational number is a real number.

Yes, every irrational number is a real number because real numbers are collection of irrational and rational numbers.

(II) Every point on the number line is of the form \sqrt{m} , where m is a natural number.

No, because every point on the number line is not form of \sqrt{m} where m is natural numbers.

let $m=1$, then Square root of $m=1$

$m=2$ " " " " $m=1.414$ - - -

$m=3$ " " " " $m=1.732$ - - -

and so on -

but what about zero, 1.111, 1.8884, 8.0, etc.

which are not been place in number line by Square root of m method.

while Number line consists infinite No. b/w two distinct digits, which are impossible to find out any function.

No Underroot function can't takes the places of number line.

Hence statement is false

(III) Every Real Number is an irrational number (F)

No, because Real Number has both Rational and Irrational Number. So Real Number would be rational or Irrational. not only irrational.

Que-2) Are the Square roots of all Positive Integers irrational? If not, give an example of the Square root of a number that is a rational number.

Solution = Square root of every Positive Integer will not yield an Integer, which are called Irrational Number.

But $\sqrt{4}$ is 2, which is an Integer. Therefore, we conclude the Square root of every Positive Integer is not an irrational number.

Que-3 = Show how $\sqrt{5}$ can be represented on the number line.

Solution = At first you need to draw a line segment AB of 2 Unit on the number line. Then draw a perpendicular line segment BC at B of 1 Unit. Then join the points C and A to form a line segment AC. According to Pythagorean triplet theorem

$$AC^2 = AB^2 + BC^2$$

$$AC^2 = 2^2 + 1^2 = 5$$

$AC = \sqrt{5}$, Then draw the arc ACD, to get the number $\sqrt{5}$ on the number line.

